

# Evaluation of the scale rate of the GNSS Terrestrial Reference Frame using satellite antenna z-offsets



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Acknowledgements: IGS ACs : CODE, ESA, NRCan, GFZ and MIT

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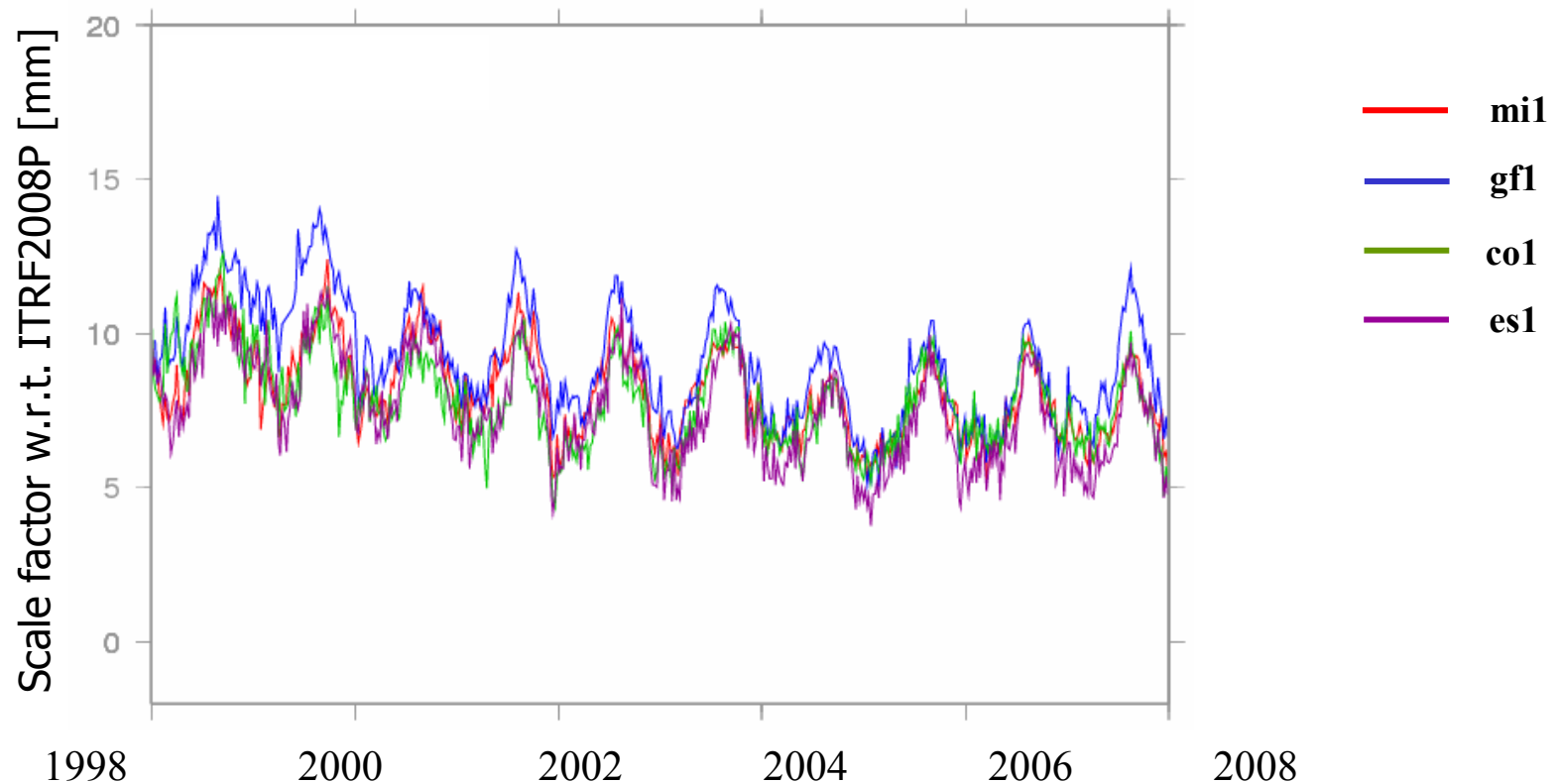
Session 2 : Strengths, weaknesses, modelling standards and processing strategies of space geodetic techniques.

## I) Introduction (1/3)

The traditional way to assess technique scales is to compute scale factor time series

-> Scale factors of 4 GPS reprocessed solutions w.r.t. ITRF2008P

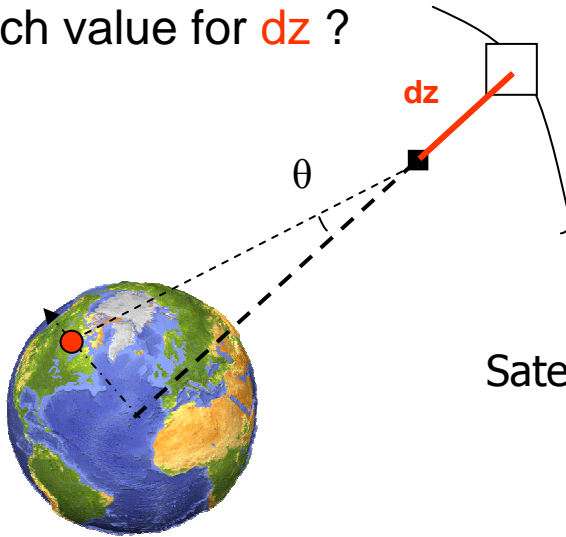
BUT these quantities depend on Satellite Antenna Phase Center Offsets (APCO)



(Collilieux et al., GPS Sol., 2010)

# I) Introduction (2/3)

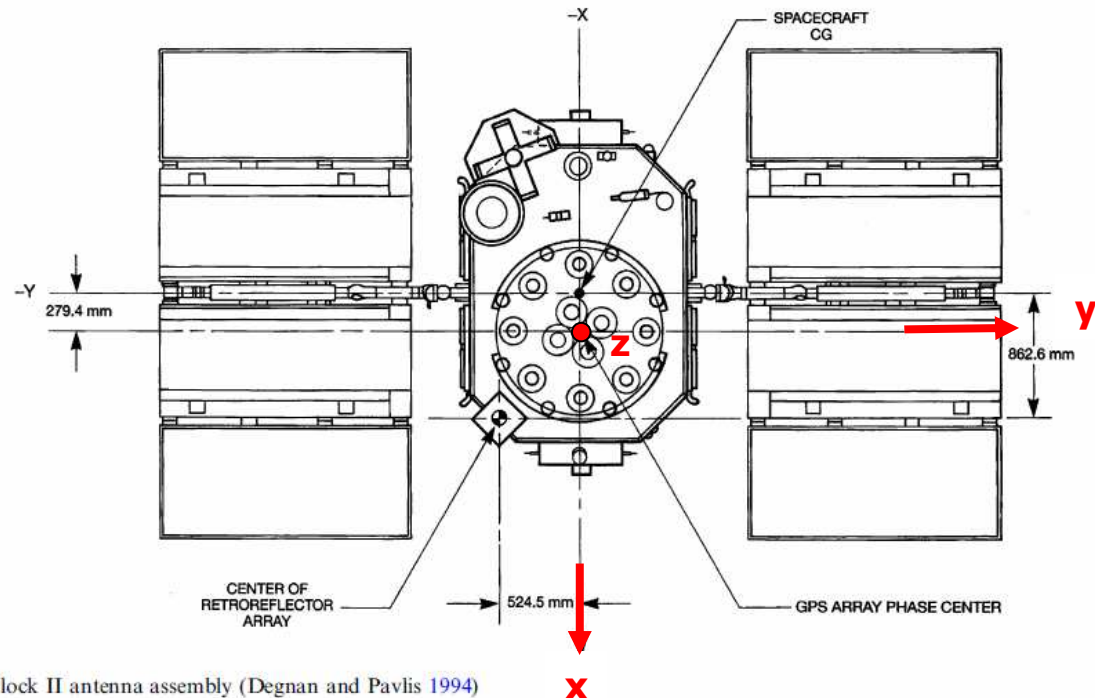
Which value for  $dz$  ?



Phase center variation : depends on the nadir ( $\theta < 14^\circ$  for GPS) and the azimuth of the signal

Phase center offset: 3 components in the satellite frame, x y and z

Satellite Antenna Phase Center position =  $PCO + PCV(\theta, Az)$



The efficiency of the corrections depends on the ability to model the satellite attitude (Dilssner, Inside GNSS, 2010)

Block II antenna assembly (Degnan and Pavlis 1994)

## I) Introduction (3/3)

Mean z-APCO are related to the TRF scale

z-APCO mean difference

$$dz(mm) = \frac{-1000}{29 + 3\epsilon_{min}^{0.75}} \cdot ds(mm) \quad (\text{Cardellach et al., JGR, 2007})$$

Scale change

Cut-off angle in degrees

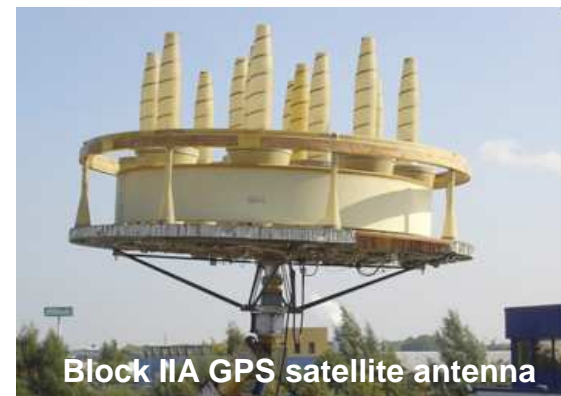
For  $\epsilon_{min} = 15^\circ$ ,

$$dz(mm) = -20 \cdot ds(mm) \quad (\text{Zhu et al., JoG, 2003})$$

An error in the mean z-APCOs of 10cm may lead to distortions in the heights of up to  $\sim 1$  mm (*Cardellach et al., JGR, 2007*)

# Outline

- I) Introduction : relationship between TRF scale and z-offsets
- II) Methodology : solving for satellite antenna z-offsets
- III) Application : evaluation of the TRF scale rate
- IV) Summary



## II) Methodology / DATA in SINEX format

	Type	Constraints	Elevation cut-off *	Comments	Data
CO1/COD	Solution (SINEX)	equality	3°	Pole constraints cannot be removed	GPS/GLONASS
ESP (ESA)	Normal Eq. (SINEX)	equality	?	-	GPS/GLONASS
EM1/EMR (NRCan)	Solution (SINEX)	Minimum constraints (orientation)	10°	Only z-APCOs available, 123 weeks rejected	GPS
GF1/GFZ	Solution (SINEX)	equality	7°	-	GPS
MI1/MIT	Solution (SINEX)	equality	10°	Single satellite APCOs fixed in certain weeks	GPS

\* ACs also use different elevation-dependent weighting strategies

**PCV estimates not contained in the SINEX files**

## II) Methodology / Using normal equations

SINEX format contains either the solution or the normal equation derived from:

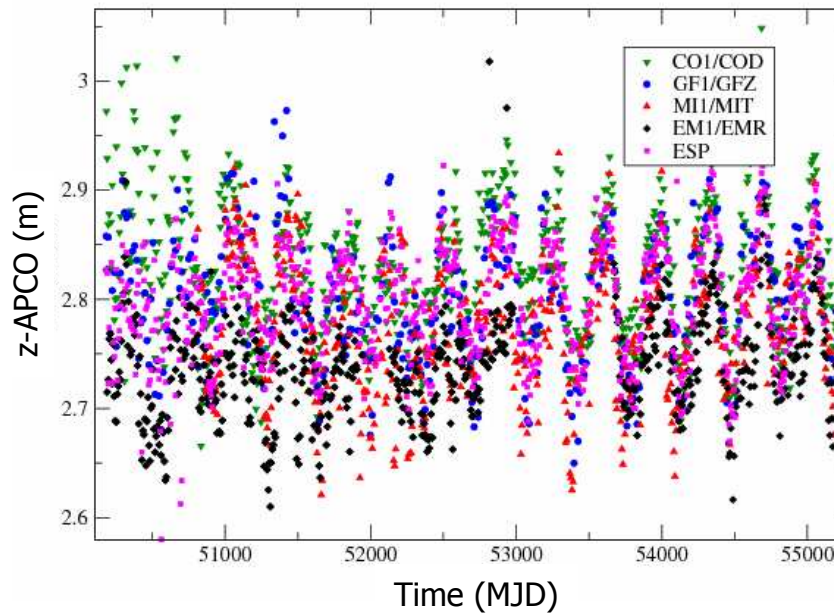
$$Y_{obs} - Y_{calc}(P_i^0) = \sum_i \frac{\partial Y}{\partial P_i} (P_i - P_i^0)$$

GPS observables of 1 week

Parameters : station positions, EOPs, x-, y- and z-APCOs, geocenter motion, (velocity)

Generally, APCO parameters are tightly constrained in the SINEX  
Due to their correlation with the TRF scale, coordinates have to be constrained if the APCO constraints are removed.

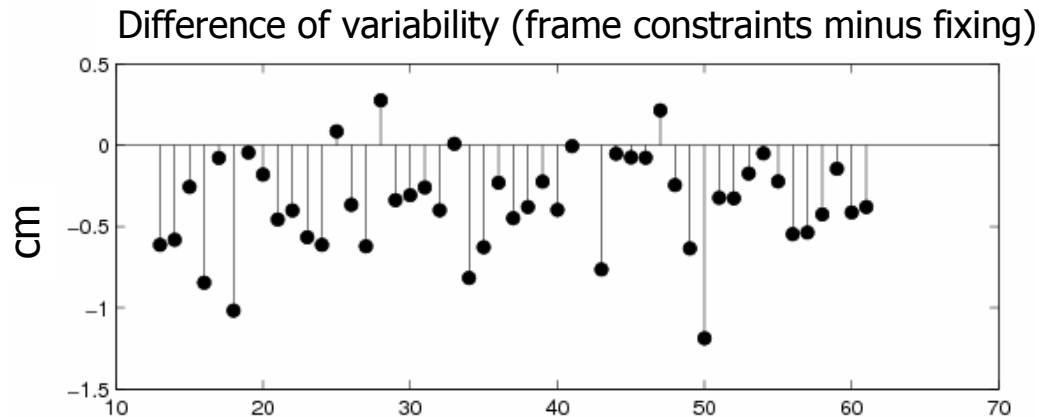
Ex. : satellite G033



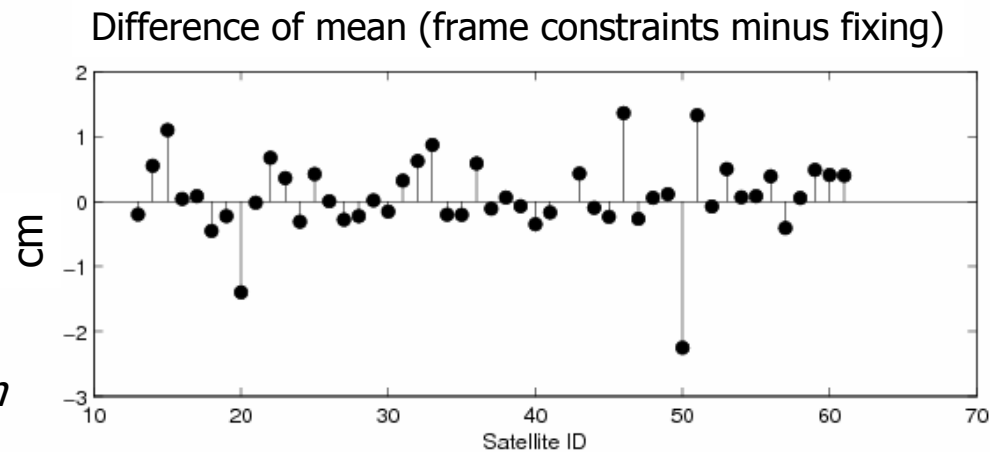
## II) Methodology

Dependence of the estimated z-APCO on the adopted strategy (1/5)

- Fixing station positions or estimating weekly coordinates (only origin, orientation and scale constrained)?



Smaller variability  
of z-APCO parameters  
if station positions are  
estimated



Differences < 1 cm if  
enough data

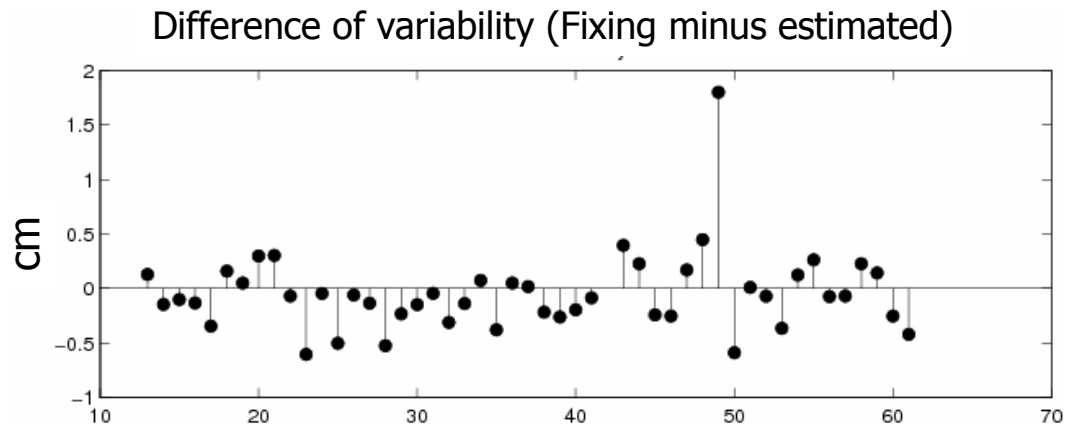
*ESP  
solution*



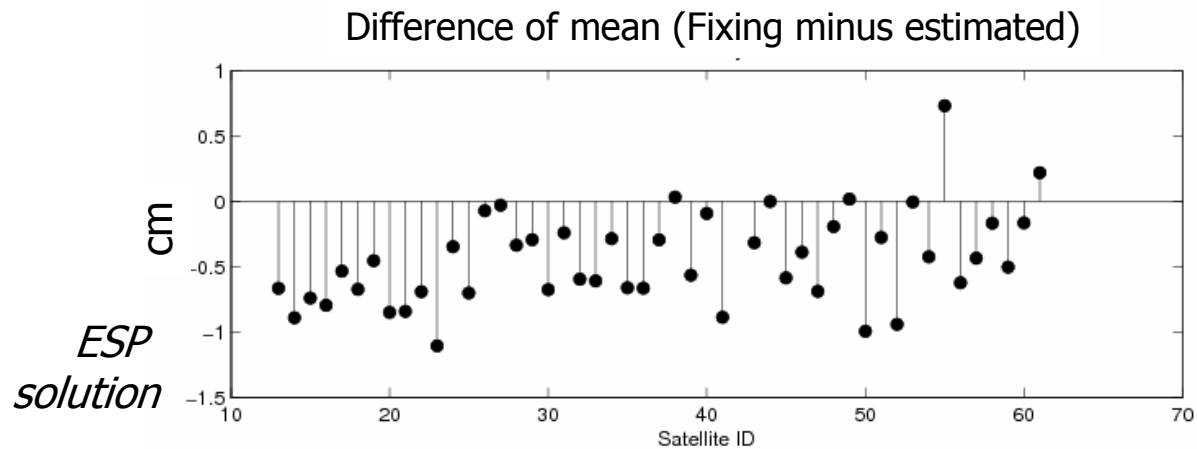
## II) Methodology

Dependence of the estimated z-APCO on the adopted strategy (2/5)

- Estimating x- and y-APCO or fixing?



Slightly smaller  
variability when x-  
and y-APCOs are  
fixed

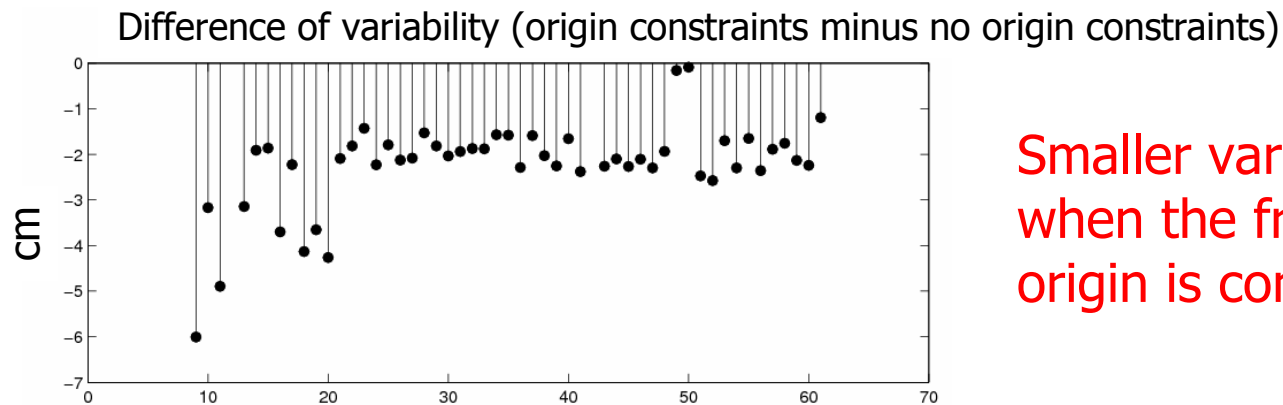


Differences < 1cm

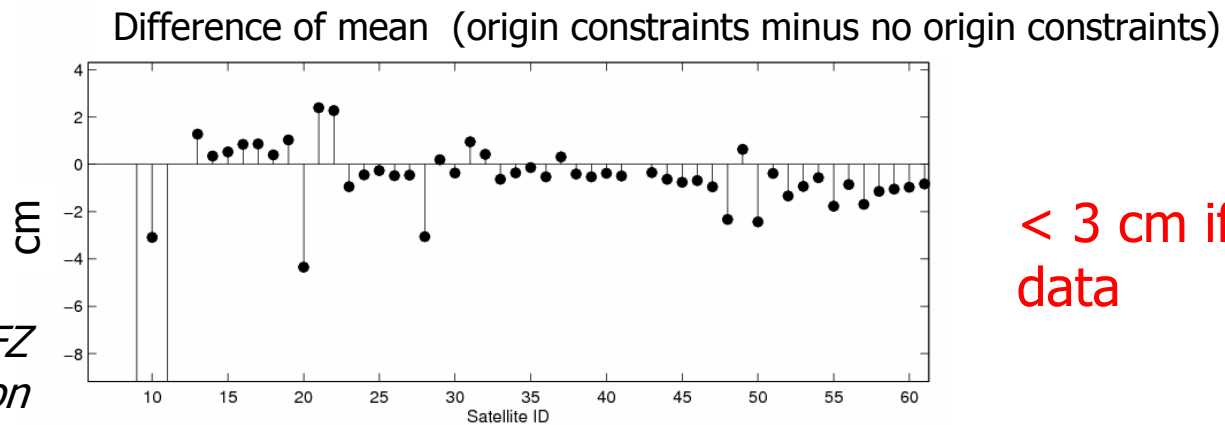
## II) Methodology

Dependence of the estimated z-APCO on the adopted strategy (3/5)

- Constraining frame origin or not?



Smaller variability  
when the frame  
origin is constrained



< 3 cm if enough  
data

*GFZ  
solution*

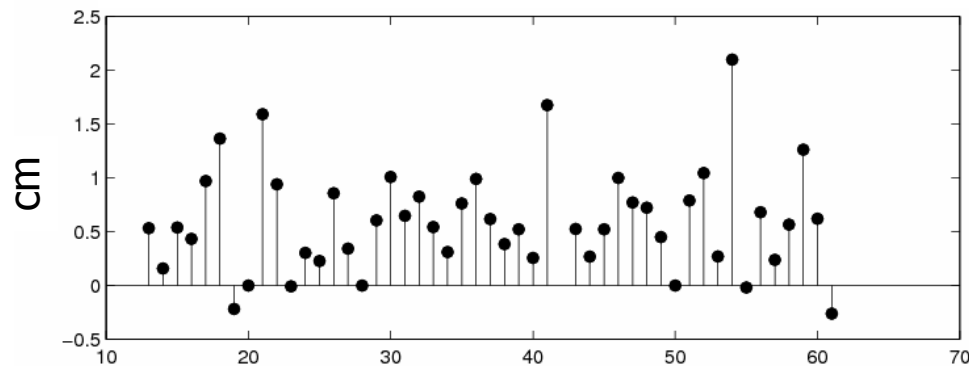
## II) Methodology

Dependence of the estimated z-APCO on the adopted strategy (4/5)

- What is the effect of fixed APCO in MIT solution?

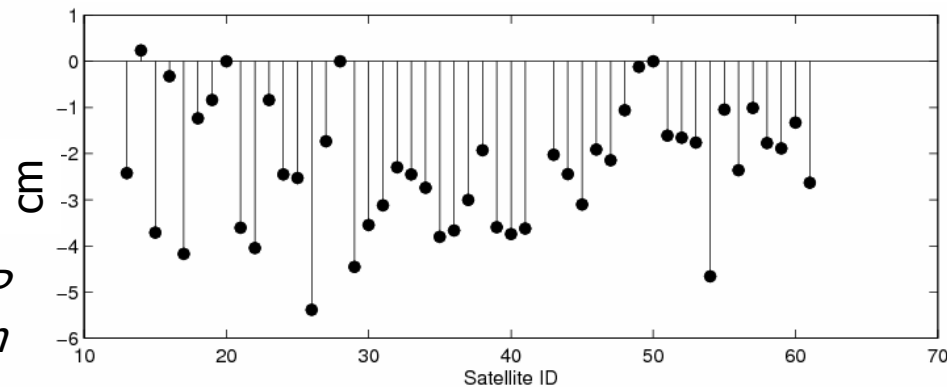
Simulations realized using ESP SINEX: same APCO fixed at the same epochs

Difference of variability (few fixed satellites minus all free)



Smaller variability when all z-APCO are estimated.

Difference of mean (few fixed satellites minus all free)



Bias of  $\sim -2$  cm

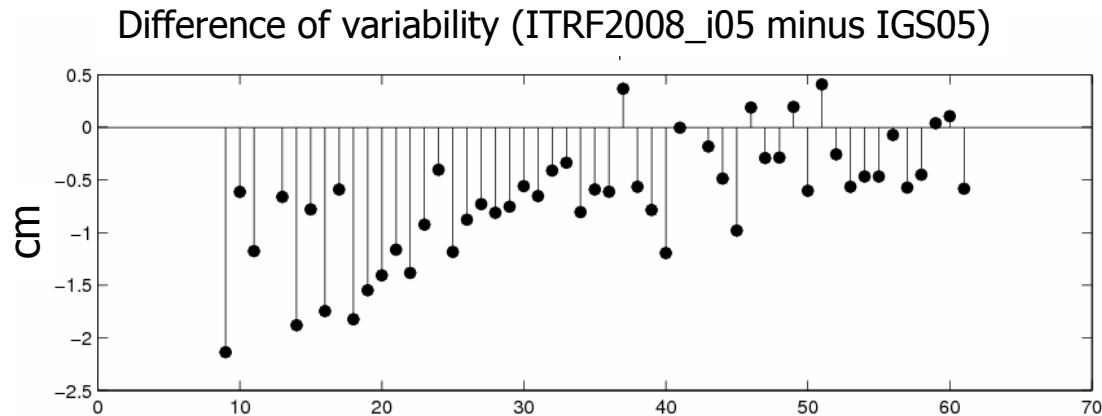
*ESP  
solution*

## II) Methodology

Dependence of the estimated z-APCO on the adopted strategy (5/5)

- Do we see any improvement when using a TRF based on ITRF2008?

ITRF2008\_i05 : derived from ITRF2008 by a 14-parameter similarity to adopt IGS05 axes



Smaller variability  
when a frame  
based on  
ITRF2008 is  
adopted



## II) Methodology

### Conclusions of these tests

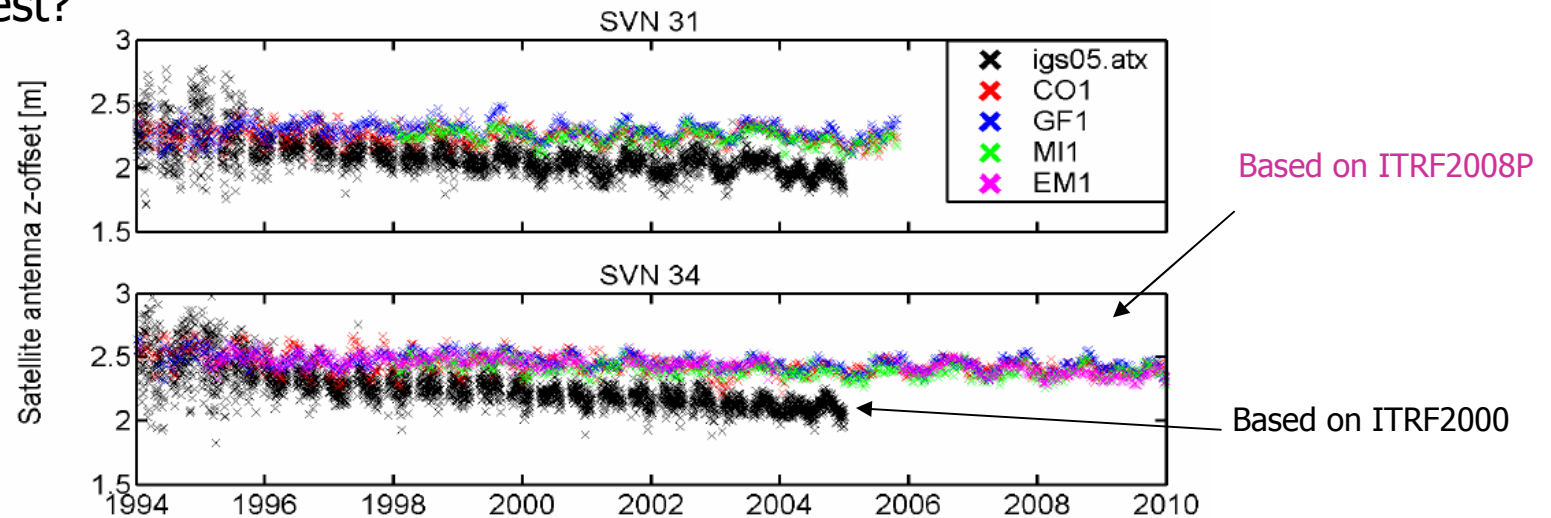
- Biases of  $\sim 3$  cm depending on the strategy
- Solution retained:
  - Frame constraints over **origin, orientation** and **scale**
  - x- and y-APCO fixed to igs05.atx
  - TRF based on the reprocessing effort: ITRF2008 (also used to get phase center corrections consistent with the future TRF)

### III) Application (1/6)

Main assumption : z-APCO estimates should be constant over time.

Which is the reference frame in which the drifts of the z-APCO parameters are the smallest?

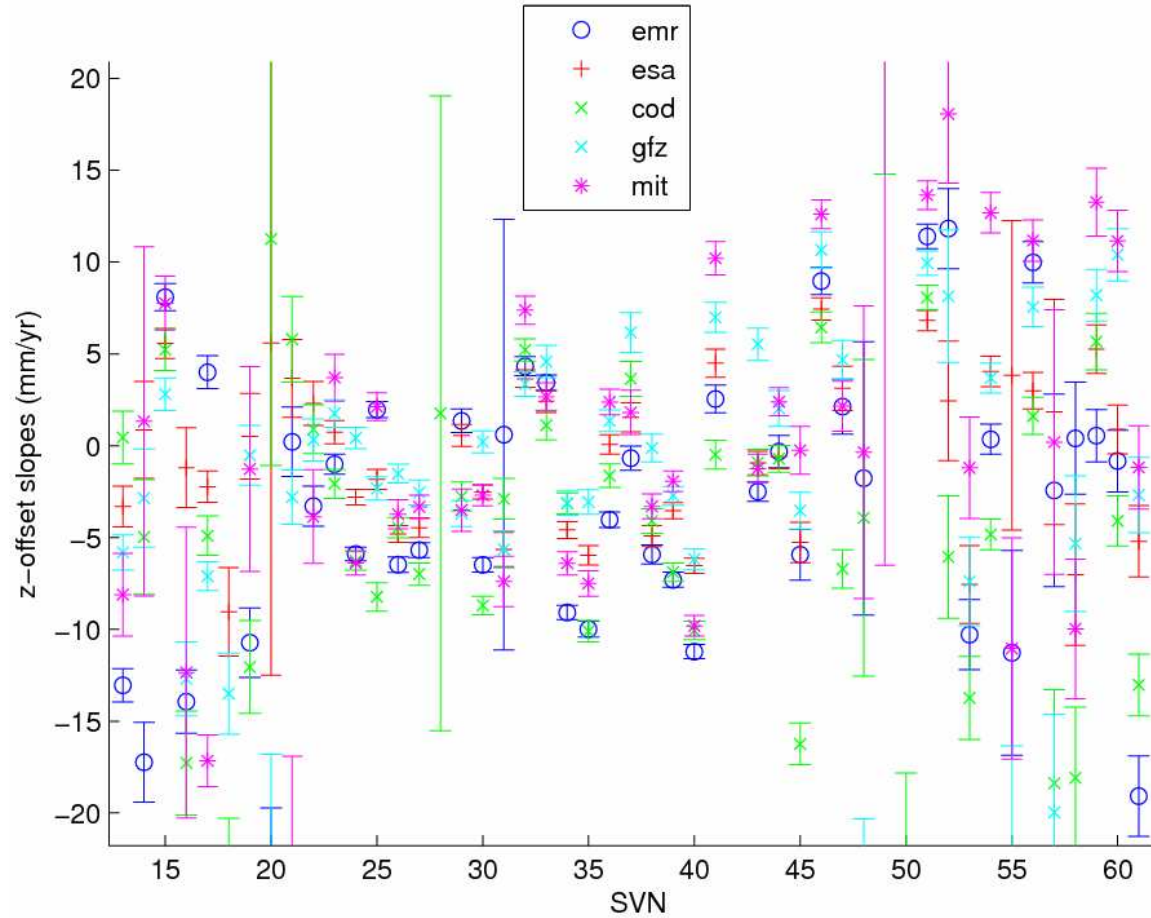
Example:



#### Limitations of the approach:

1) Satellite center of mass might change due to mass loss (fuel used for maneuvers). For Block IIA satellites, **-4.6 mm** in the Z direction for the expected **lifetime** of the satellite (*Degnan and Pavlis, GPS World, 1994*). Probably a theoretical number?

### III) Application (2/6)

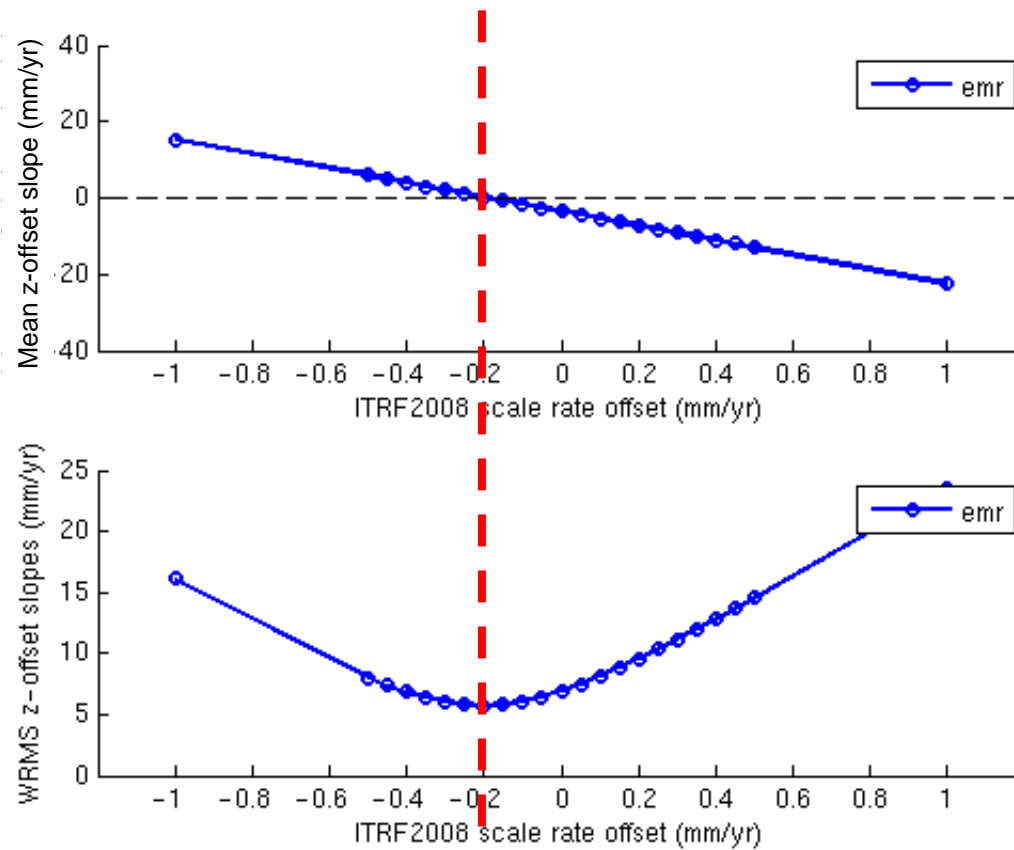


Limitations of the approach:

2) The drift depends on the satellite and on the AC

### III) Application (3/6)

We derived various TRFs from ITRF2008 by changing only scale drift

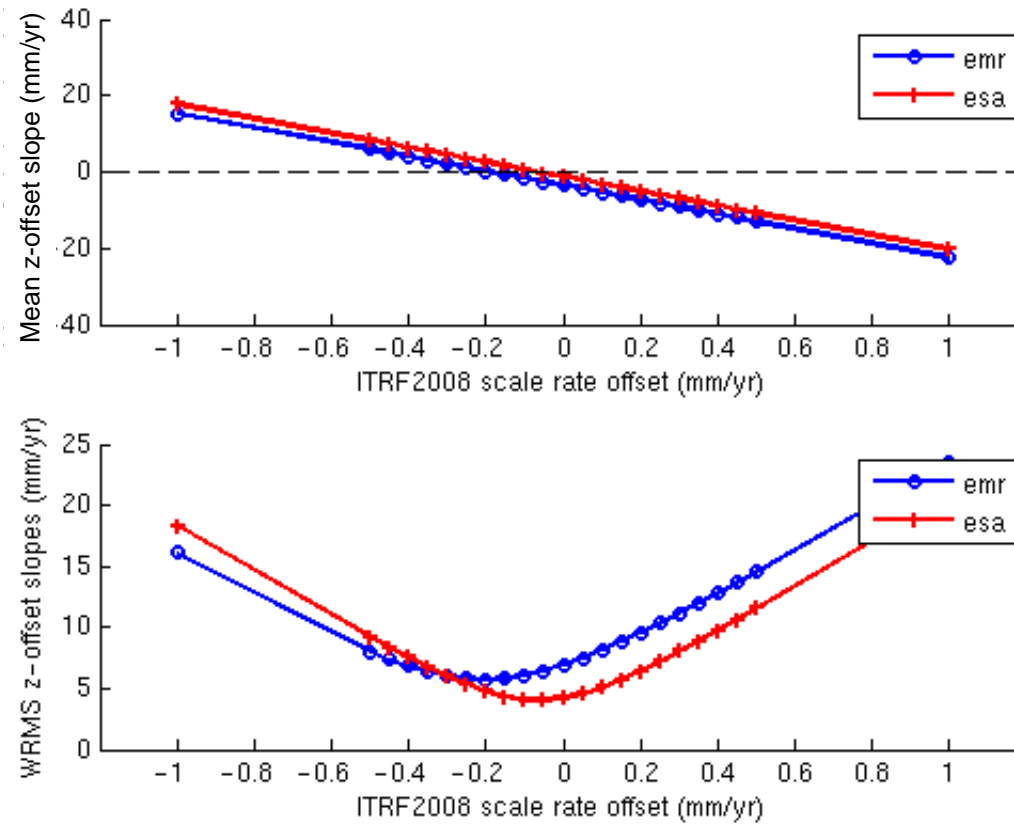


The z-offset drifts are different depending on the TRF scale



### III) Application (3/6)

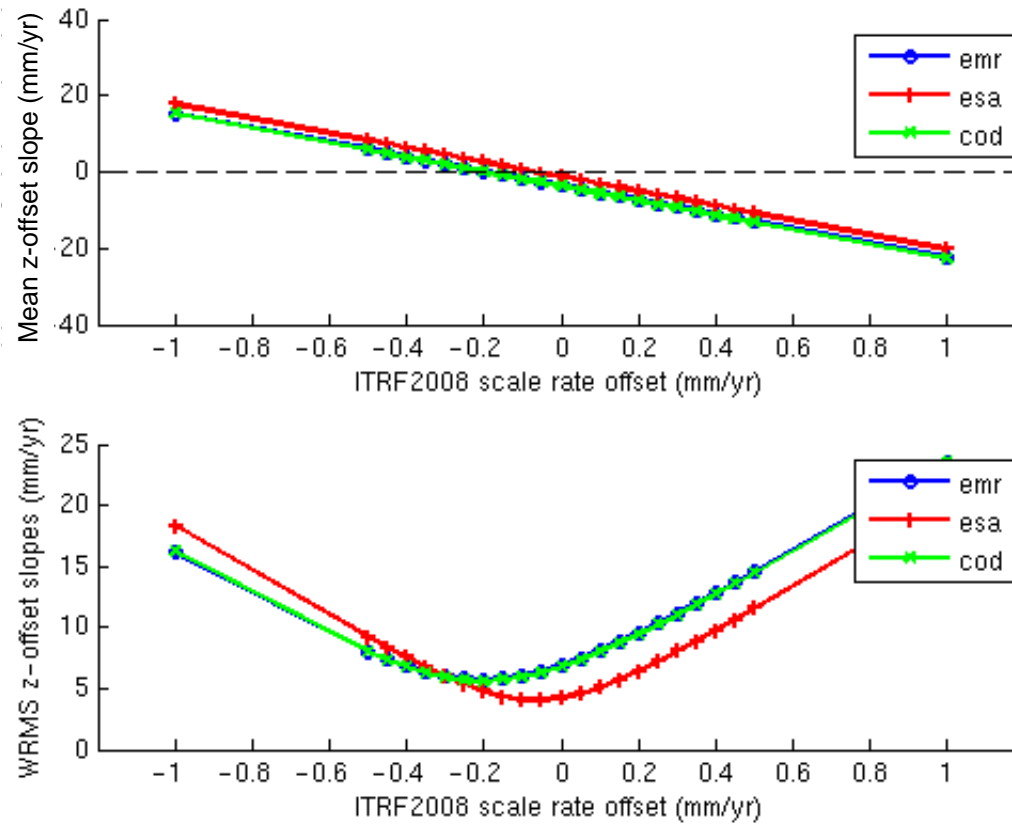
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The z-offset drifts are different depending on the TRF scale

### III) Application (3/6)

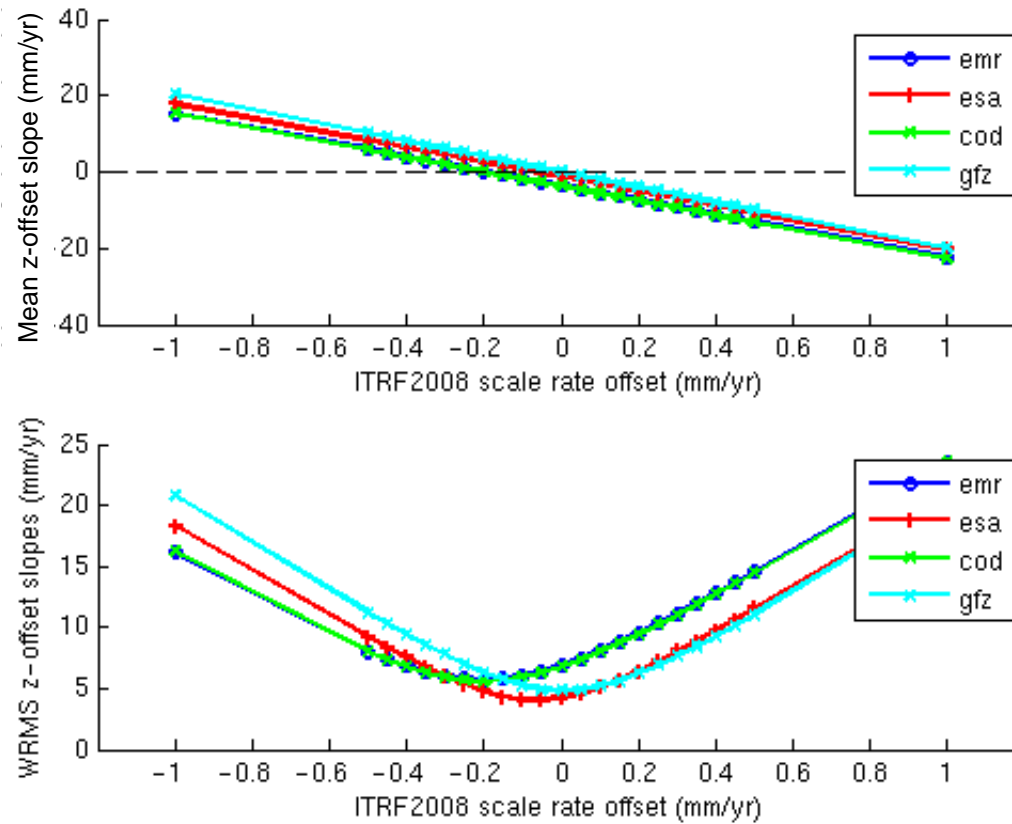
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The z-offset drifts are different depending on the TRF scale

### III) Application (3/6)

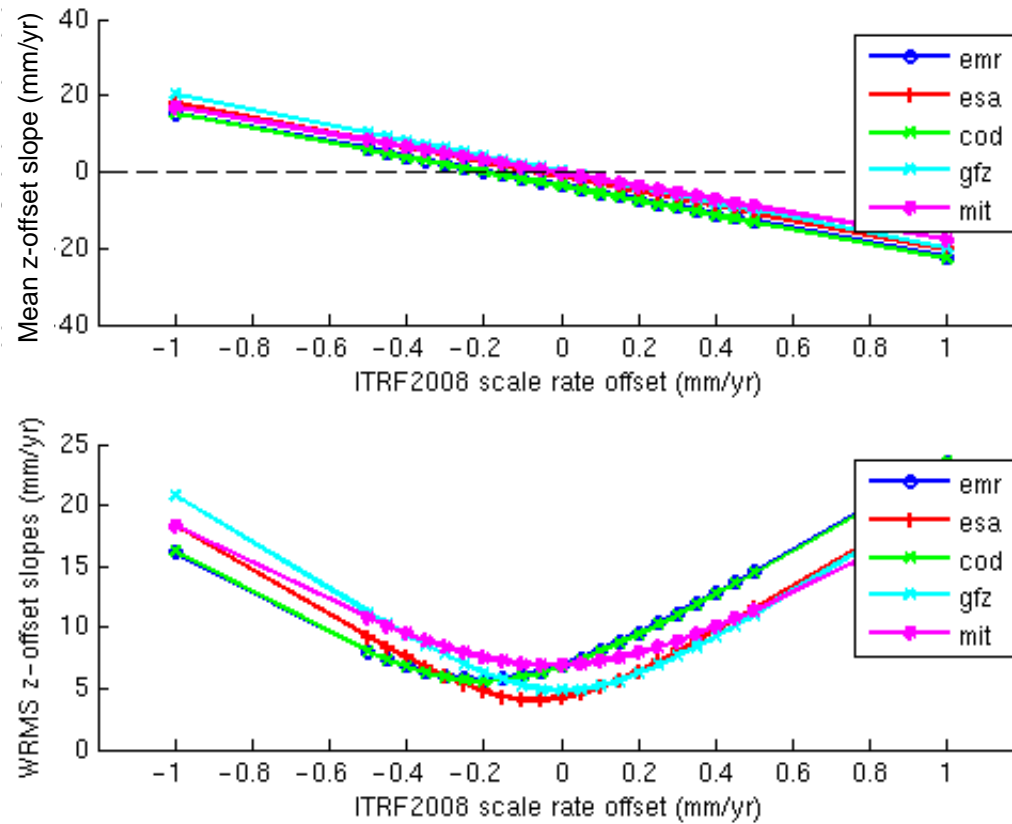
We derived various TRFs from ITRF2008 by changing only scale drift



The z-offset drifts are different depending on the TRF scale

### III) Application (3/6)

We derived various TRFs from ITRF2008 by changing only scale drift



The z-offset drifts are different depending on the TRF scale

### III) Application (4/6)

Conclusion on ITRF2008 scale drift

$$-0.2 \text{ mm/yr} \leq \text{intrinsic GPS scale} \leq 0.0 \text{ mm/yr}$$

SLR scale drift w.r.t. ITRF2008 is :  $-0.15 \text{ mm/yr}$  (*Z. Altamimi, pers. comm.*)

VLBI scale drift w.r.t. ITRF2008 is :  $0.15 \text{ mm/yr}$

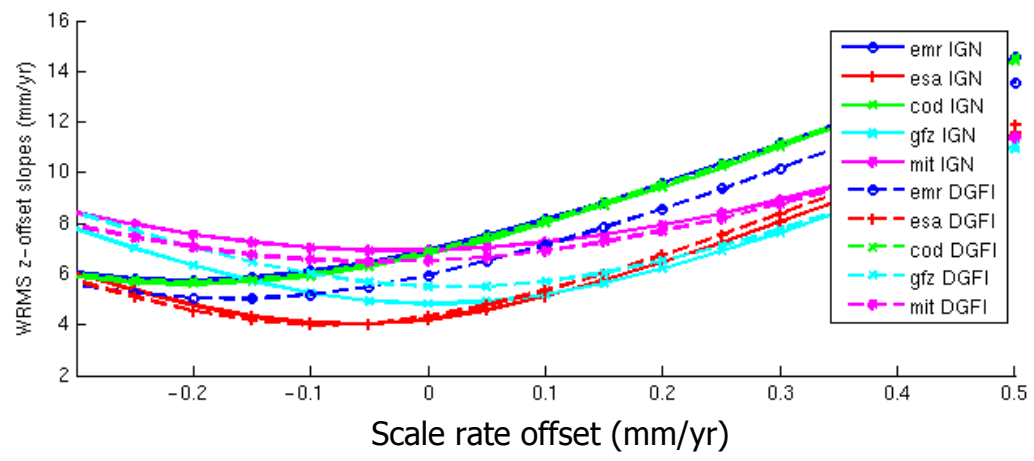
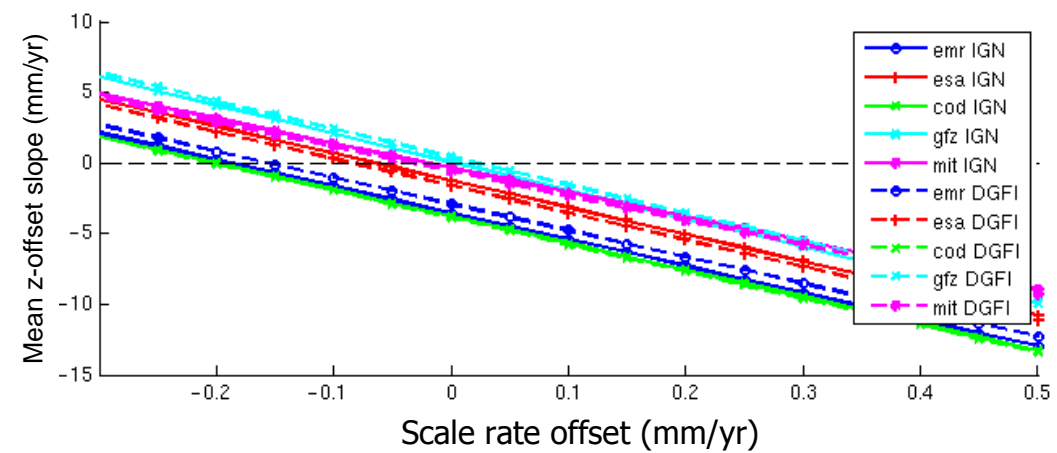
GPS intrinsic scale may be slightly closer to SLR scale, but confirms ITRF2008 choice of adopting SLR and VLBI mean scale.

Is this test appropriate to evaluate different reference frame solutions?

**Not really, it depends on the AC solution**

### III) Application (5/6)

Difference between IGN TRF (ITRF2008) and DGFI TRF



### III) Application (6/6)

Transformation parameters between ITRF2008 and DGFI Reference Frame. **No scale drift.**

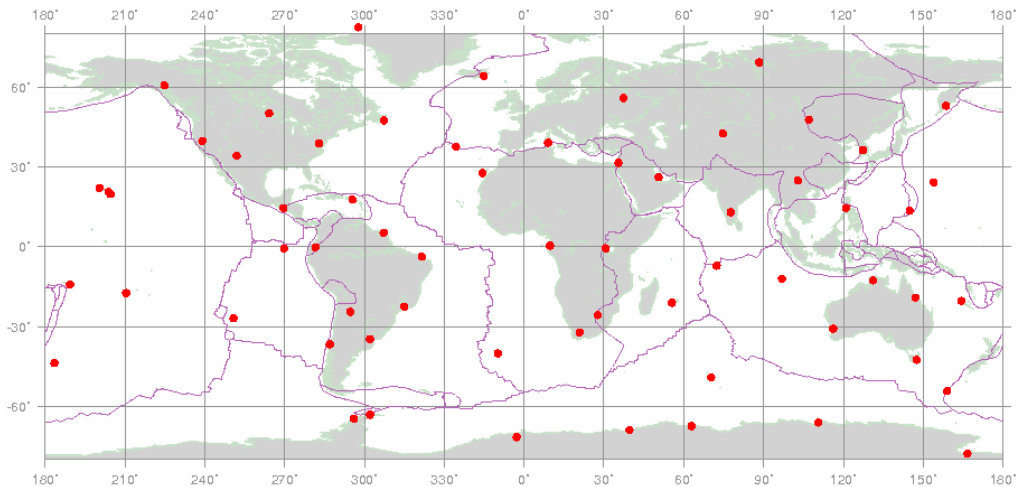
Solution	T1	T2	T3	D	R1	R2	R3	Epoch
	mm	mm	mm	10 <sup>-9</sup>	mas	mas	mas	y
-----								
Rates	0.1	0.0	-0.1	-0.02	0.002	0.002	-0.004	
+/-	0.1	0.1	0.1	0.02	0.004	0.005	0.004	

Based on GPS sites only

Core network (courtesy of P. Rebischung)

Rejection up to normalized residuals > 6.0

Non-weighted



# Summary

## Methodology

- Biases of  $\sim 3$  cm depending on the strategy
- Solution retained:
  - Frame constraints over **origin, orientation and scale**
  - x- and y-APCO fixed to igs05.atx
  - TRF based on the reprocessing effort: ITRF2008

## Conclusion on ITRF2008 scale drift

**$-0.2 \text{ mm/yr} \leq \text{intrinsic GPS scale} \leq 0.0 \text{ mm/yr}$**

- GPS intrinsic scale may be slightly closer to SLR scale, but confirms ITRF2008 choice of adopting SLR and VLBI mean scale
- DGFI and IGN reference frame scale rates perform similarly